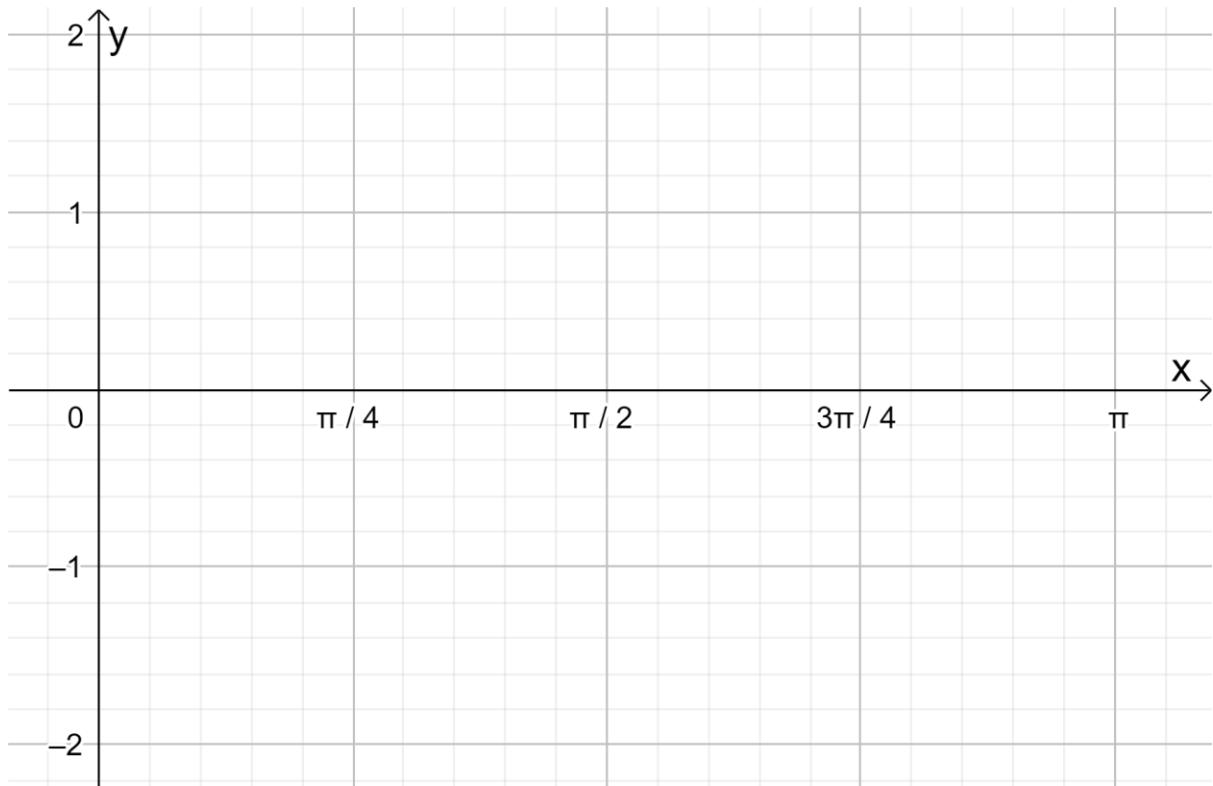


Let $f(x) = (\cos 2x - \sin 2x)^2$

a) Show that $f(x)$ can be expressed as $1 - \sin 4x$

b) Let $f(x) = 1 - \sin 4x$. Sketch the graph of f for $0 \leq x \leq \pi$



a)

$$\begin{aligned}f(x) &= (\cos 2x - \sin 2x)^2 \\&= (\cos 2x - \sin 2x)(\cos 2x - \sin 2x) \\&= \cos^2 2x - 2\cos 2x \sin 2x + \sin^2 2x\end{aligned}$$

$$\cos^2 \theta + \sin^2 \theta \equiv 1 \quad 2\cos^2 x + \cos x - 1 = 0$$

Therefore

$$\begin{aligned}\cos^2 2x + \sin^2 2x &\equiv 1 \\&= 1 - 2\cos 2x \sin 2x\end{aligned}$$

$$\sin 2\theta \equiv 2\sin \theta \cos \theta$$

Therefore

$$\begin{aligned}\sin 4x &\equiv 2\sin 2x \cos 2x \\&= 1 - \sin 4x\end{aligned}$$

b)

Consider the graph $y = \sin x$

Stretch by a factor of $\frac{1}{4}$ in the x direction

Reflect in the x axis

Translate up 1 unit

