

a) Show that  $\cos 2\theta - 3\cos \theta + 2 \equiv 2\cos^2 \theta - 3\cos \theta + 1$

b) Hence, solve  $\cos 2\theta - 3\cos \theta + 2 = 0$  for  $0 \leq \theta \leq 2\pi$

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a)

$$\cos 2\theta - 3\cos \theta + 2$$

$$\cos 2\theta \equiv 2\cos^2 \theta - 1$$

$$\cos 2\theta - 3\cos \theta + 2 \equiv 2\cos^2 \theta - 1 - 3\cos \theta + 2$$

$$\cos 2\theta - 3\cos \theta + 2 \equiv 2\cos^2 \theta - 3\cos \theta + 1$$

b)

$$\cos 2\theta - 3\cos \theta + 2 = 0$$

$$2\cos^2 \theta - 3\cos \theta + 1 = 0$$

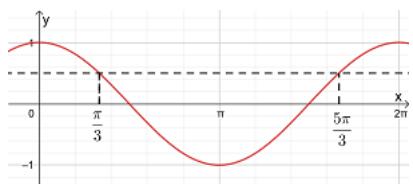
$$(2\cos \theta - 1)(\cos \theta - 1) = 0$$

$$\cos x = \frac{1}{2}, \cos x = 1$$

$$\arccos\left(\frac{1}{2}\right) = \frac{\pi}{3}$$

$$\arccos(1) = 0$$

Solve  $0 \leq x \leq 2\pi$



$$x = 0, \frac{\pi}{3}, \frac{5\pi}{3}, 2\pi$$